

Semester One Examination, 2021

SOLUTIONS

Question/Answer booklet

MATHEMATICS METHODS UNIT 1

Section One: Calculator-free

WA student number: In fig



In words

Number of additional answer booklets used

(if applicable):



Materials required/recommended for this section

To be provided by the supervisor This Question/Answer booklet Formula sheet

Time allowed for this section

Reading time before commencing work:

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: nil

Working time:

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

five minutes

fifty minutes

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	52	35
Section Two: Calculator-assumed	13	13	100	98	65
				Total	100

Instructions to candidates

- 1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer booklet preferably using a blue/black pen. Do not use erasable or gel pens.
- 3. You must be careful to confine your answers to the specific question asked and to follow any instructions that are specific to a particular question.
- 4. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 5. It is recommended that you do not use pencil, except in diagrams.
- 6. Supplementary pages for planning/continuing your answers to questions are provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

(6 marks)

Section One: Calculator-free

This section has **eight** questions. Answer **all** questions. Write your answers in the spaces provided.

3

Working time: 50 minutes.

Question 1

Solve the following equations for x.

(2x+5)(x-4) = 0.(2 marks) (a) Solution $2x + 5 = 0 \Rightarrow x = -\frac{5}{2} = -2.5$ $x - 4 = 0 \Rightarrow x = 4$ $x = -2.5, \quad x = 4$ **Specific behaviours** ✓ first correct solution ✓ second correct solution (b) $x^2 - 10x - 11 = 0.$ (2 marks) Solution (x-11)(x+1) = 0*x* = 11 x = -1, **Specific behaviours** ✓ indicates correct method ✓ both correct solutions $(x-8)^2 - 100 = 0.$ (2 marks) (c) **Solution** $(x-8)^2 = 10^2$ $x - 8 = \pm 10$ x = 18, x = -2**Specific behaviours** ✓ indicates correct method ✓ both correct solutions

METHODS UNIT 1

Question 2

The straight line *L* has equation 4x + 2y = 1.

(a) Write the equation of L in the form y = mx + c to show that its gradient is -2. (1 mark)

4

Solution
$2y = -4x + 1 \Rightarrow y = -2x + \frac{1}{2} \Rightarrow m = -2$
Specific behaviours
\checkmark correct values of <i>m</i> and <i>c</i>

Line L_1 is perpendicular to L and passes through the point (2, 6).

Line L_2 is parallel to L and passes through the point (1, -7).

(b) Determine the point of intersection of L_1 and L_2 .

Solution $L_{1}:(y-6) = \frac{1}{2}(x-2) \Rightarrow y = \frac{1}{2}x+5$ $L_{2}:(y-1) = -2(x--7) \Rightarrow y = -2x-5$ $\frac{1}{2}x+5 = -2x-5$ $(\frac{1}{2}+2)x = -10$ $\frac{5}{2}x = -10$ x = -4 $y = \frac{1}{2}(-4) + 5 = 3$ Lines intersect at (-4,3). Specific behaviours \checkmark gradient of L_{1} \checkmark equation of L_{2} \checkmark equates lines and groups like terms \checkmark solves for x \checkmark solves for y and states point of intersection (7 marks)

(6 marks)



UNIT 1



(3 marks)

Consider the function $f(x) = \frac{p}{x+q}$, where *p* and *q* are constants. The graph of y = f(x) has an asymptote with equation x = 2 and passes through the point (6, -1).

6

(a) Determine the value of p and the value of q.



(b) State the equation of the other asymptote of the graph of y = f(x). (1 mark)

Solution
y = 0
Specific behaviours
✓ correct equation

(c) Sketch the graph of y = f(x) on the axes below.

(3 marks)



Mark on the circumference of the circle the points *P* and *Q* so that rays drawn from the origin to each point make clockwise angles of 285° and $\frac{7\pi}{12}$ from the positive *x*-axis respectively.



7

WIT 1

ME

y

(7 marks)

Determine the number of possible combinations when three students must be chosen (a) from a small class of six. (2 marks)

8



Determine the coefficient of the x^3 term in the expansion of (b)

(i)
$$(2x+3)^3$$
.

$$2x + 3)^{3}.$$
(2 marks)
$$\begin{pmatrix} 3\\0 \end{pmatrix} (2x)^{3} (3)^{0} = 8x^{3}$$
Coefficient is 8.
$$\underbrace{\text{Specific behaviours}}_{\checkmark \text{ indicates method}}$$

$$\checkmark \text{ indicates coefficient}$$

 $(3x - 10)^6$. (ii)

(3 marks)



Two polynomial functions are defined by f(x) = (2x - 3)(x + 2) and $g(x) = x^3 + 4x^2 - 4x - 12$.

Determine the coordinates of the point(s) of intersection of f(x) and g(x).

	Solution
E	xpand $f(x)$
	f(x) = (2x - 3)(x + 2)
	$=2x^2+x-6$
_	
E	quate functions:
	$x^3 + 4x^2 - 4x - 12 = 2x^2 + x - 6$
E	quate to zero:
	$x^3 + 2x^2 - 5x - 6 = 0$
F	ind root:
1	$r = -1 \rightarrow -1 + 2 + 5 = 6 = 0$
	$x = -1 \Rightarrow -1 + 2 + 3 - 0 = 0$
S	tart factorising:
	$x^{3} + 2x^{2} - 5x - 6 = (x + 1)(x^{2} + x - 6)$
С	complete factorising:
	$x^{3} + 2x^{2} - 5x - 6 = (x + 1)(x + 3)(x - 2)$
С	coordinates:
	f(-1) = (-5)(1) = -5
	f(-3) = (-9)(-1) = 9
	f(2) = (1)(4) = 4
Ir	itersect at $(-1, -5)$, $(-3, 9)$ and $(2, 4)$.
	Specifie bebavieure
√	expands quadratic
~	equate functions and then to zero
\checkmark	finds first root
~	factors into linear and quadratic
	completes factorisation
~	
✓ ✓	determines v -coordinates and states coordinates of all point



Supplementary page

Question number: _____